

Catalan's constant G results

The following results are Polynomial Continued Fractions of the Catalan constant. For the results marked as "new and unproven", we have not found any formal proof yet.

Novelty	Formula	Polynomials	Convergence $\frac{\text{digits}}{\text{term}}$
known	$\frac{6}{-\pi \operatorname{acosh}(2)+8G} = 2 - \frac{2}{19 - \frac{108}{56 - \frac{108}{113 - \frac{108}{244}}}}$	$a_n = 10n^2 + 7n + 2, b_n = -(2n-1)^4 - (2n-1)^3$	0.60046
new and unproven	$\frac{1}{2G} = 1 - \frac{2}{7 - \frac{19}{19 - \frac{109}{37 - \frac{109}{224}}}}$	$a_n = 3n^2 + 3n + 1, b_n = -2n^4$	0.298
new and unproven	$\frac{2}{2G-1} = 1 - \frac{4}{7 - \frac{19}{19 - \frac{18}{37 - \frac{18}{247}}}}$	$a_n = 3n^2 + 3n + 1, b_n = -2n^3(n+1)$	0.28903
new and unproven	$\frac{24}{18G-11} = 1 - \frac{6}{7 - \frac{19}{19 - \frac{64}{37 - \frac{64}{268}}}}$	$a_n = 3n^2 + 3n + 1, b_n = -2n^3(n+2)$	0.27984
new and unproven	$\frac{720}{450G-299} = 1 - \frac{8}{7 - \frac{19}{19 - \frac{80}{37 - \frac{80}{292}}}}$	$a_n = 3n^2 + 3n + 1, b_n = -2n^3(n+3)$	0.27042
new and unproven	$\frac{2}{2G-1} = 3 - \frac{6}{13 - \frac{19}{29 - \frac{64}{51 - \frac{64}{268}}}}$	$a_n = 3n^2 + 7n + 3, b_n = -2n^3(n+2)$	0.30387
new and unproven	$\frac{4}{2G+1} = 3 - \frac{12}{13 - \frac{19}{29 - \frac{12}{51 - \frac{12}{268}}}}$	$a_n = 3n^2 + 7n + 3, b_n = -2n^2(n+1)(n+2)$	0.29507
new and unproven	$\frac{16}{6G-1} = 3 - \frac{18}{13 - \frac{19}{29 - \frac{18}{51 - \frac{18}{268}}}}$	$a_n = 3n^2 + 7n + 3, b_n = -2n^2(n+2)^2$	0.28608
new and unproven	$\frac{288}{90G-31} = 3 - \frac{24}{13 - \frac{19}{29 - \frac{24}{51 - \frac{24}{268}}}}$	$a_n = 3n^2 + 7n + 3, b_n = -2n^2(n+2)(n+3)$	0.27687
new and unproven	$\frac{1}{2-2G} = 7 - \frac{16}{19 - \frac{108}{37 - \frac{108}{61 - \frac{108}{140}}}}$	$a_n = 3n^2 + 9n + 7, b_n = -2n(n+1)^3$	0.30672
new and unproven	$\frac{24}{18G-11} = 5 - \frac{10}{19 - \frac{10}{39 - \frac{10}{65 - \frac{10}{192}}}}$	$a_n = 3n^2 + 11n + 5, b_n = -2n^3(n+4)$	0.30966
new and unproven	$\frac{16}{6G-1} = 5 - \frac{20}{19 - \frac{10}{39 - \frac{20}{65 - \frac{20}{192}}}}$	$a_n = 3n^2 + 11n + 5, b_n = -2n^2(n+1)(n+4)$	0.30103
new and unproven	$\frac{64}{18G+13} = 5 - \frac{30}{19 - \frac{10}{39 - \frac{30}{65 - \frac{30}{192}}}}$	$a_n = 3n^2 + 11n + 5, b_n = -2n^2(n+2)(n+4)$	0.29221
new and unproven	$\frac{4}{6G-5} = 9 - \frac{18}{23 - \frac{18}{43 - \frac{18}{69 - \frac{18}{144}}}}$	$a_n = 3n^2 + 11n + 9, b_n = -2n^2(n+2)^2$	0.30958
new and unproven	$\frac{8}{3-2G} = 9 - \frac{36}{23 - \frac{18}{43 - \frac{36}{69 - \frac{36}{144}}}}$	$a_n = 3n^2 + 11n + 9, b_n = -2n(n+1)(n+2)^2$	0.30095
new and unproven	$\frac{32}{2G+5} = 9 - \frac{54}{23 - \frac{18}{43 - \frac{54}{69 - \frac{54}{144}}}}$	$a_n = 3n^2 + 11n + 9, b_n = -2n(n+2)^3$	0.29213
new and unproven	$\frac{192}{18G+13} = 9 - \frac{72}{23 - \frac{18}{43 - \frac{72}{69 - \frac{72}{144}}}}$	$a_n = 3n^2 + 11n + 9, b_n = -2n(n+2)^2(n+3)$	0.28311
new and unproven	$\frac{6}{17-18G} = 13 - \frac{32}{29 - \frac{32}{51 - \frac{32}{79 - \frac{32}{140}}}}$	$a_n = 3n^2 + 13n + 13, b_n = -2n(n+1)^2(n+3)$	0.31239
new and unproven	$\frac{48}{90G-79} = 15 - \frac{30}{33 - \frac{30}{57 - \frac{30}{87 - \frac{30}{146}}}}$	$a_n = 3n^2 + 15n + 15, b_n = -2n^2(n+2)(n+4)$	0.31522
new and unproven	$\frac{32}{19-18G} = 15 - \frac{40}{33 - \frac{30}{57 - \frac{40}{87 - \frac{40}{146}}}}$	$a_n = 3n^2 + 15n + 15, b_n = -2n(n+1)(n+2)(n+4)$	0.30674
new and unproven	$\frac{128}{17-6G} = 15 - \frac{90}{33 - \frac{30}{57 - \frac{90}{87 - \frac{90}{146}}}}$	$a_n = 3n^2 + 15n + 15, b_n = -2n(n+2)^2(n+4)$	0.29808
new and unproven	$\frac{8}{54G-49} = 19 - \frac{64}{37 - \frac{64}{61 - \frac{64}{91 - \frac{64}{124}}}}$	$a_n = 3n^2 + 15n + 19, b_n = -2n(n+2)^3$	0.31515
new and unproven	$\frac{12}{83-90G} = 23 - \frac{64}{43 - \frac{64}{69 - \frac{64}{101 - \frac{64}{124}}}}$	$a_n = 3n^2 + 17n + 23, b_n = -2n(n+1)(n+3)^2$	0.31792